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# Thermal expansion of $\mathbf{M g}(\mathbf{O H})_{2}$ brucite under high pressure and pressure dependence of entropy 

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#### Abstract

An equation of state for $\mathrm{Mg}(\mathrm{OH})_{2}$ brucite under high-pressure and high-temperature conditions has been obtained by measuring temperature dependence of volume up to 600 K at ambient pressure and pressure dependence of volume up to 16 GPa at 300 , 473, 673, and 873 K with in situ X-ray diffraction. Pressure dependence of entropy of brucite has been calculated with thermal expansion coefficient and volume which are derived from the present EoS. This dependence indicates that generation of secondary OH dipoles affects entropy. The OH dipoles probably appear around 2 GPa and the number seems not to change over 8 GPa at 300 K .


Keywords Brucite • Equation of state • Thermal expansion • Entropy • X-ray diffraction

## Introduction

$\mathrm{Mg}(\mathrm{OH})_{2}$ brucite is one of the simplest solids which have hydroxyl groups. It has a hexagonal crystal structure (Zigan and Rothbauer 1967) with space group $P \overline{3} m 1$. Brucite has been studied to understand hydrogen behavior and the nature of hydrogen bonding in solid and to understand the compression behavior of layered dense magnesium hydrous silicates (DMHS) because an

[^0]$\mathrm{Mg}(\mathrm{OH})_{6}$ unit is regarded as a part of a DMHS structure (Kudoh et al. 1993).

Spectroscopy techniques (Kruger et al. 1989; Duffy et al. 1995; Shinoda and Aikawa 1998; Shinoda et al. 2002) and neutron diffraction (Parise et al. 1994) were applied to $\mathrm{Mg}(\mathrm{OH})_{2}$ and $\mathrm{Mg}(\mathrm{OD})_{2}$ in order to investigate the behavior of hydrogen and deuteron, respectively. Both types of experiments showed that a secondary OH dipole is formed with compression and that hydrogen prefers the $6 i$ position to the $2 d$, which hydrogen occupies under ambient conditions. The site change of hydrogen from $2 d$ to $6 i$ was also reported on $\mathrm{Ca}(\mathrm{OH})_{2}$ (Desgranges et al. 1993). The effect of the change of hydrogen site in $\mathrm{Ca}(\mathrm{OH})_{2}$ appeared on the thermal expansion coefficient at one-atmosphere condition. The site change is called hydrogen motion.

Equations of state (EoS) for brucite were reported using X-ray diffraction by many groups (Fei and Mao 1993; Catti et al. 1995; Duffy et al. 1995; Xia et al. 1998; Nagai et al. 2000). There is, however, no report that a hydrogen behavior such as mentioned above affects the lattice system of brucite. One of the reasons is that only its compression behavior was discussed so far. The effect may appear as a thermal effect on the lattice system just as reported for portlandite (Fukui et al. 2003). The thermal expansion has to be determined precisely in order to discuss the effect.

We report the thermo-elastic properties of $\mathrm{Mg}(\mathrm{OH})_{2}$ brucite obtained through in situ X-ray observations at high temperature and high pressure. Using these results, the temperature dependence of thermal expansion at constant pressure is discussed.

## Experimental

Ambient pressure experiments
To obtain reference volumes at ambient pressure, $V_{0}$, which is a parameter for EoS, X-ray diffraction observations at high temperature were carried out with XRD-DSC II (Rigaku Corp). The degree of temperature fluctuation is below 0.2 K . Temperature
calibrations were performed by detecting the melting reactions of indium ( 429.81 K ), tin ( 505.168 K ), and lead ( 600.702 K ). The optical system was refined using a silicon diffraction pattern with $\mathrm{Cu} K \alpha_{1}$ radiation.

The dehydration temperature was confirmed before X-ray observations. X-ray diffraction patterns were collected from just below the dehydration temperature to room temperature at about every 50 K . Commercial reagent of $99.9 \%$ purity $\mathrm{Mg}(\mathrm{OH})_{2}$ powder with brucite structure produced by Iwatani Chemical Ltd. was used as a starting sample. X-ray diffraction patterns were collected at air-atmosphere condition. The sample was filled into an aluminum plate. The heating/cooling rate for this experiment was $5 \mathrm{Kmin}^{-1}$.

High-pressure experiments
In situ X-ray diffraction observations under high pressure were done up to 23 GPa at 300 K and to 16 GPa at higher temperature using the SPEED-1500 system installed at BL04B1, SPring-8 (Utsumi et al. 1998). Eight tungsten carbide cubes with truncation edge length of 3 mm were used as the second-stage anvils. The pressure-transmitting medium was sintered magnesium oxide and the gasket material was pyrophillite. A cell assemblage of Irifune et al. (1998) was used with modifications. In order to prevent the sample from reacting with the pressure medium of magnesium oxide, we introduced a sample chamber made of graphite which was confirmed in advance not to react with brucite up to 6 GPa and 1500 K . Figure 1 shows the central part of the cell. The sample chamber was put between a pair of heater sheets made of cemented TiC-diamond powders. The starting material was a mixture of brucite and gold powders $\left[\mathrm{Mg}(\mathrm{OH})_{2}: \mathrm{Au}=10: 1\right.$ in weight ratio]. Initial diameters of the capsule were 2 mm inside and 3 mm outside. Disks of magnesium oxide were put between the graphite capsule and TiC heaters for electric insulation. White X-rays collimated by horizontal ( $0.05-\mathrm{mm}$ ) and vertical $(0.1-\mathrm{mm})$ slits were directed to a sample position very close to the junction of a thermocouple. The position was confirmed with X-ray radiography using a CCD camera. The diffracted beam, collimated by a $0.05-\mathrm{mm}$ horizontal slit, was detected with a pure germanium solid-state detector attached on a horizontal rotating goniometer. The data collection was performed with typical duration of 600 s at the two-theta angle of $4.7^{\circ}$. Pressure was estimated from the unit-cell volume of gold using the equation of state (Anderson et al. 1989). Temperature was monitored with a thermocouple of W97\%Re3\%-W75\%Re25\%. Pressure effects on emf were ignored. Temperature fluctuation was less than 1 K during the exposure time. The sample was compressed and then heated to 900 K and kept at that temperature for more than 10 min . Diffraction patterns were collected on a cooling cycle. Because deviatoric stress relaxed once the sample was heated above the target temperature, the obtained data were free from such complicating effects.

## Results and discussion

## Thermal expansion at ambient pressure

The dehydration temperature of brucite was determined to be 600.6 K . A representative X-ray diffraction pattern


Fig. 1 Central part of the high pressure cell. Heaters are placed below and above the sample space. Other parts are shown in the figure
is shown in Fig. 2. Lattice constants were refined with four diffraction lines from (001), (100), (101), and (102) planes using the least-squares method. Calculated lattice parameters, the unit-cell volume, and $c / a$ ratio are shown in Table 1 and plotted in Fig. 3. The values of $a$ and $c$ vary smoothly in this temperature range. The $c / a$ ratio also varies continuously. The datasets from 299 to 592 K were used to calculate the thermal expansion coefficients. The coefficients were calculated with the following equation:
$l=l_{0} \exp \left[\int_{T_{0}=300 K}^{T} \alpha_{l} \mathrm{~d} T\right]$,
where $l$ is a length of $a$, or $c$, or volume, and $l_{0}$ is its value at the standard temperature, $T_{0} . T_{0}$ is 300 K in this study. $\alpha$ is a thermal expansion coefficient. Obtained values of $a, c$, and volume are listed in Table 2. The obtained thermal expansion coefficient for volume is shown with previous results in Table 3. Though the values are very similar around 300 K , that by Redfern and Wood (1992) is considerably larger at the hightemperature region than those of the others. They reported that the lattice parameters at 293 K were 3.149 and $4.749 \AA$ for the $a$ axis and $c$ axis, respectively. The value of the $a$ axis is larger than reported by the others and those of JCPDS, while that of the $c$ axis is smaller. This fact means that Redfern and Wood underestimated the unit-cell volume at the standard state. Consequently, the thermal expansion coefficient was overestimated.


Fig. 2 X-ray profile of $\mathrm{Mg}(\mathrm{OH})_{2}$ obtained at 299.5 K and ambient pressure

Table 1 Refined lattice parameters and volume of brucite under ambient conditions

| $T(\mathrm{~K})^{\mathrm{a}}$ | $a(\AA)$ | $c(\AA)$ | $c / a$ | $V\left(\AA^{3}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| 299.3 | $3.1476(4)^{\mathrm{a}}$ | $4.7705(6)$ | 1.5156 | $40.930(12)$ |
| 299.3 | $3.1477(7)$ | $4.7694(10)$ | 1.5152 | $40.925(22)$ |
| 349.2 | $3.1481(16)$ | $4.7807(25)$ | 1.5186 | $41.031(47)$ |
| 356.4 | $3.1486(13)$ | $4.7867(15)$ | 1.5203 | $41.096(37)$ |
| 397 | $3.1490(7)$ | $4.7902(10)$ | 1.5212 | $41.136(22)$ |
| 418 | $3.1507(3)$ | $4.7979(4)$ | 1.5228 | $41.247(10)$ |
| 456.6 | $3.1514(11)$ | $4.8098(13)$ | 1.5262 | $41.367(31)$ |
| 469.8 | $3.1521(6)$ | $4.8063(8)$ | 1.5248 | $41.356(18)$ |
| 515.1 | $3.1532(2)$ | $4.8215(2)$ | 1.5291 | $41.516(5)$ |
| 571.5 | $3.549(7)$ | $4.8348(9)$ | 1.5325 | $41.675(20)$ |
| 592.9 | $3.1550(8)$ | $4.8411(10)$ | 1.5344 | $41.732(23)$ |

[^1]

Fig. 3a-d Axial and volume data of $\operatorname{Mg}(\mathrm{OH})_{2}$ as function of temperature at ambient pressure. a $a$ axis. b $c$ axis. c $c / a$ ratio. d Volume

Those by the others are consistent even at high temperature.

Isothermal elastic properties
A representative diffraction pattern of $\mathrm{Mg}(\mathrm{OH})_{2}$ brucite acquired at high pressure is shown in Fig. 4. Lattice parameters of $\mathrm{Mg}(\mathrm{OH})_{2}$ under each condition were derived from $d$ values for at least four lines out of (001), (100), (101), (102), (110), and (111) planes. Obtained lattice parameters at 300 K are listed in Table 4. The volume compression data are plotted in Fig. 5. The bulk modulus and its pressure derivative at zero pressure can be calculated by fitting the third-order Birch-Murnaghan equation of state (Birch 1947) to the pressurevolume data:

Table 2 Obtained lattice constants and volume of brucite at 300 K

| $a_{0}\left[\AA \AA^{\mathrm{A}}\right]$ | $3.1472(2)$ |
| :--- | :---: |
| $c_{0}[\mathrm{~A}]$ | $4.7699(11)$ |
| $V_{0}\left[\mathrm{~A}^{3}\right]$ | $40.917(12)$ |

$$
\begin{align*}
P= & \frac{3}{2} K_{0}\left[\left(\frac{V_{0}}{V}\right)^{\frac{7}{3}}-\left(\frac{V_{0}}{V}\right)^{\frac{5}{3}}\right] \\
& \cdot\left\{1+\frac{3}{4}\left(K_{0}^{\prime}-4\right) \cdot\left[\left(\frac{V_{0}}{V}\right)^{\frac{2}{3}}-1\right]\right\} . \tag{2}
\end{align*}
$$

The calculated bulk modulus and its pressure derivative are shown in Table 5 with previous results. The calculated compression curve and previous data are also shown in Fig. 5. The results of room temperature compression are consistent with each other.

Data obtained under high-temperature and high pressure conditions are listed in Table 4 and plotted in Fig. 6. Equation (2) was fitted to the compression data with fixed $V_{0}$ values which are calculated with thermal expansion at ambient pressure. Obtained isothermal elastic parameters, $K_{T 0}$ and $K_{T 0}$ are listed in Table 6. The compression curves are also shown in Fig. 6. These curves show good agreement with measured volumes. Figure 6 also shows pressure-volume data reported by Xia et al. (1998) with open squares and their compression curves with dotted lines. Both curves of the present result and their result are very consistent, whereas there is a difference between the curves at 873 K at the lowpressure region as shown in Fig. 6c. We believe that the present observation is more accurate than that by Xia et al. (1998) for the following reasons. (1) Pressure marker was mixed with sample. (2) The thermocouple junction was located at the center of the sample. (3) The temperature fluctuation and gradient are very small. (4) Obtained diffraction data came from an area very close to the junction.

Temperature dependence of bulk modulus and its pressure derivative at ambient pressure were calculated by fitting the following equation $B=(\partial B / \partial T)_{P=0}$ $\cdot(T-300)+B_{T=300}$, where $B,(\partial B / \partial T)_{P=0}$, and $B_{T=300}$ show $K_{T 0}$ or $K_{T 0}$, the temperature derivative at zero pressure, and the value at 300 K , respectively. Consequently, the value of $\left(\partial K_{T} / \partial T\right)_{P=0}$ was obtained as $-0.0319(29)$ and that of $\left(\partial K_{T} / \partial T\right)_{P=0}$ as $0.00571(45)$.

Pressure dependences of thermal expansion coefficient and entropy

Thermal expansion coefficients at constant pressure were obtained by fitting Eq. (1) to four volumes under each

Table 3 Thermal expansion coefficients of brucite ${ }^{\mathrm{a}}$

| $\alpha_{0}\left(\times 10^{-5} 1 \mathrm{~K}^{-1}\right)$ | $\alpha_{1}\left(\times 10^{-7} 1 \mathrm{~K}^{-2}\right)$ | Temperature <br> range (K) | Reference |
| :--- | :--- | :--- | :--- |
| 0.23 | 2.37 | $293-583$ | Redfern and Wood (1992) |
| 8.0 | - | $300-650$ | Fei and Mao (1993) |
| 7.3 | 0.36 | - | Xia et al. (1998) |
| $6.69(18)^{\mathrm{b}}$ | - | $299-592$ | This study |

[^2]

Fig. 4 X-ray diffraction profile of $\mathrm{Mg}(\mathrm{OH})_{2}$ obtained at 300 K and 16.05 GPa. Bru and $A u$ indicate diffraction lines from $\mathrm{Mg}(\mathrm{OH})_{2}$ brucite and gold, respectively
pressure condition. These volumes were calculated with the elastic parameters shown in Table 5.

Since the thermal expansion coefficient has been obtained, we can calculate the pressure dependence of entropy at constant temperature using a relation $(\partial S / \partial P)_{T}=-\alpha V$, where $S, P, T, \partial$, and $V$ are entropy, pressure, temperature, thermal expansion coefficient, and volume, respectively. The obtained values are plotted in Fig. 7. $(\partial S / \partial P)_{T}$ has large negative values under lower pressure conditions. As pressure increases, the
absolute value decreases. The slope of $(\partial S / \partial P)_{T}$ at 300 K is almost constant from ambient pressure to 2 GPa and becomes smaller from 3 to 7 GPa . Above 8 GPa, $\left(\partial^{2} S / \partial P^{2}\right)_{T}$ is a little negative or almost zero. The pressure range where the gradient changes is consistent with the pressure where a newly IR absorption peak appears (Shinoda and Aikawa 1998). These results imply the following:

1. Entropy decreases with pressure.
2. The absolute value of $(\partial S / \partial P)_{T}$ is large below 3 GPa and decreases above this pressure. This can be understood by considering two pressure effects on configuration and vibration of the OH dipole. Contribution of configurational entropy increases with pressure because the hydrogen atoms that form the secondary OH dipole occupy one of three $6 i$ sites. Because the frequency of the secondary OH bonding is smaller than that of the original OH bonding and the vibrational entropy change is expressed as $\Delta S=k_{B} \ln \left(v / v^{\prime}\right) \cdot$ oscillator $^{-1}$, where $k_{B}$ is the Boltzman constant, when the frequency changes from $v$ to $v^{\prime}$, the frequency decrease from original OH to secondary OH causes entropy to increase. Both effects of configuration and vibration involved with the

Table 4 Refined lattice parameters and volume of brucite
${ }^{\text {a }}$ Figures in parentheses for lattice parameters and volume indicate estimated standard deviations of the last significant digit. Those for pressure were errors estimated from the standard deviations of the lattice parameter of gold

| $T$ (K) | $P\left(\mathrm{GP}_{\mathrm{a}}\right)$ | $a(\AA)$ | $c(\AA)$ | $c / a$ | $V\left(\AA^{3}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 300 | $-0.06(13)^{\mathrm{a}}$ | 3.1450 (12) | $4.7773(31)$ | 1.5190 | 40.922(43) |
| 300 | 0.00(6) | 3.1445 (15) | 4.7773(26) | 1.5192 | $40.909(50)$ |
| 300 | 4.00 (7) | 3.0990 (10) | 4.5773(24) | 1.4771 | 38.069(32) |
| 300 | 5.80(6) | 3.0791 (5) | $4.5002(11)$ | 1.4615 | $36.950(15)$ |
| 300 | 7.32(8) | 3.0643(5) | $4.4588(12)$ | 1.4551 | 36.258(16) |
| 300 | 7.50 (13) | $3.0702(71)$ | 4.4424(160) | 1.4470 | 36.264(212) |
| 300 | 10.35(10) | 3.0380 (8) | 4.3984(17) | 1.4478 | $35.156(24)$ |
| 300 | 13.44(13) | 3.0141 (2) | 4.3421 (6) | 1.4406 | 34.162(7) |
| 300 | 14.38(11) | $3.0101(14)$ | $4.3384(31)$ | 1.4413 | 34.043(40) |
| 300 | 16.05(12) | 2.9971(9) | $4.3166(21)$ | 1.4403 | 33.579(27) |
| 300 | 18.26(15) | $2.9824(23)$ | $4.2836(58)$ | 1.4363 | $32.996(64)$ |
| 300 | 19.86(10) | $2.9662(19)$ | 4.2657(43) | 1.4381 | $32.502(53)$ |
| 300 | 22.56(12) | $2.9532(14)$ | 4.2444 (33) | 1.4372 | $32.058(41)$ |
| 473 | 9.59(11) | 3.0448 (19) | $4.4055(37)$ | 1.4469 | 35.371(54) |
| 473 | 11.36(9) | $3.0294(10)$ | $4.3651(33)$ | 1.4409 | 34.694(34) |
| 473 | 13.43(12) | 3.0148 (32) | 4.3464 (74) | 1.4417 | 34.212(93) |
| 473 | 15.15(15) | $3.0027(26)$ | $4.3064(49)$ | 1.4342 | $33.626(70)$ |
| 473 | 16.52(7) | 2.9907 (80) | 4.2957(211) | 1.4364 | 33.437(242) |
| 473 | 5.95 (3) | 3.0780 (3) | 4.4953(7) | 1.4605 | 36.883(10) |
| 473 | 8.28(7) | $3.0584(168)$ | 4.4548(319) | 1.4566 | 36.088(474) |
| 473 | 10.24(5) | 3.0411(29) | $4.3967(56)$ | 1.4458 | 35.214(81) |
| 673 | 9.07(6) | 3.0520 (28) | 4.4291 (66) | 1.4512 | $35.729(85)$ |
| 673 | 11.00 (5) | 3.0350 (29) | 4.3861(40) | 1.4451 | $34.979(75)$ |
| 673 | $13.05(5)$ | $3.0222(2)$ | 4.3510 (5) | 1.4397 | 34.416 (7) |
| 673 | 14.56 (6) | $3.0043(42)$ | $4.3274(56)$ | 1.4404 | 33.826(104) |
| 673 | 16.09(12) | $2.9985(33)$ | 4.3211(116) | 1.4411 | 33.647(117) |
| 673 | 5.62(5) | 3.0852(11) | $4.5225(32)$ | 1.4659 | 37.280(38) |
| 673 | 7.96 (5) | $3.0629(9)$ | 4.4600 (39) | 1.4561 | $36.235(38)$ |
| 673 | $9.85(6)$ | 3.0441 (29) | 4.4144(47) | 1.4502 | 35.426 (77) |
| 873 | 8.75(4) | 3.0540(8) | 4.4670 (19) | 1.4627 | 36.081(24) |
| 873 | 10.46 (3) | 3.0367 (7) | 4.4172(21) | 1.4546 | 35.276(24) |
| 873 | 12.44(11) | $3.0237(16)$ | 4.3887(22) | 1.4515 | 34.749 (31) |
| 873 | 14.00(9) | $3.0080(36)$ | 4.3748(126) | 1.4544 | 34.280(128) |
| 873 | 15.48(5) | $3.0010(37)$ | $4.3451(51)$ | 1.4479 | 33.890 (72) |
| 873 | 5.21(5) | 3.0875(7) | 4.5660 (19) | 1.4789 | 37.695(23) |
| 873 | 7.52(4) | 3.0659(8) | 4.4951(23) | 1.4662 | 36.593(26) |
| 873 | 9.49(6) | 3.0493(14) | 4.4519(27) | 1.4600 | 35.848(39) |



Fig. 5 Volume compression data shown by inverted triangles and compression curve of brucite at 300 K in this study. Previous results are shown by circles (Catti et al. 1995); squares (Duffy et al. 1995); diamonds (Xia et al. 1998), and triangles (Nagai et al., 2000)

Table 5 Bulk moduli and their pressure derivatives of brucite at 300 K

| $K_{T 0}(\mathrm{GPa})$ | $K_{T 0}$, | Method | Reference |
| :--- | :--- | :--- | :--- |
| 54.3 | 4.7 | PXD $^{\text {a }}$ | Fei and Mao (1993) |
| 47 | 4.7 (fixed) | PND $^{\mathrm{b}}$ | Parise et al. (1994) |
| 42 | 5.7 | SCXD $^{\mathrm{c}}$ | Duffy et al. (1995) |
| 39 | 7.6 | PND $^{\text {PND }}$ | Catti et al. (1995) |
| 36.7 | - | B $^{\mathrm{d}}$ | Xia et al. (1998) |
| 39.6 | 6.7 | PXD | Xia et al. (1998) |
| 44 | 6.7 (fixed) | PXD | Nagai et al. (2000) |
| $41.8(1.3)$ | $6.6(3)$ | PXD | This study |

[^3]hydrogen transition therefore make the absolute value of $(\partial S / \partial P)_{T}$ decrease.
3. The value does not change much above 8 GPa . This means that all hydrogen atoms have formed the secondary OH dipole.
The variation $(\partial S / \partial P)_{T}$ for brucite has been compared with that for periclase, into which brucite dehydrates, and which does not have a phase transition in this pressure range. The values for periclase were calculated with the reported parameters (Dewaele et al. 2000). These are shown also in Fig. 7. There is no slope change on $(\partial S / \partial P)_{T}$ though the value decreases little by little with pressure due to the effect of pressure on the vibration. This is consistent with the fact that no phase transition has so far been reported for periclase in this pressure range.

Through these experiments, hydrogen behavior obviously has been found to affect the lattice system. This transition of hydrogen in brucite is not a first-order phase transition but a higher one. It is, however, not mentioned what the order the transition is. Though $\left(\partial^{2} S / \partial P^{2}\right)_{T}$ seems not to show discontinuity at any pressure but to change continuously because smooth functions were used to model the relationship between volume, pressure, and temperature, there is still a possibility that $\left(\partial^{2} S / \partial P^{2}\right)_{T}$ has a discontinuity. To confirm this more precise measurement, that is probably very difficult with the present instruments, is needed.


Fig. 6a-c Volume compression data of brucite under high-temperature conditions a 473 K. b 673 K. c 873 K. Solid circles and curves indicate the results of this study, and open squares and dotted curves are those from Xia et al. (1998)

Table 6 Isothermal bulk moduli and the pressure derivatives of brucite at high temperature

| $T(\mathrm{~K})$ | $K_{T 0}(\mathrm{GPa})$ | $K^{\prime}{ }_{T 0}$ |
| :--- | :--- | :--- |
| 300 | $41.8(1.3)$ | $6.6(4)$ |
| 473 | $32.6(2.5)$ | $8.3(1.1)$ |
| 673 | $28.8(2.1)$ | $9.0(1.1)$ |
| 873 | $23.9(1.4)$ | $10.0(0.9)$ |



Fig. 7 Pressure derivative of entropy at 300 K. Circles and squares are for brucite and for periclase, respectively. The inset shows the values for periclase

## Conclusion

The EoS for brucite has been determined precisely in the range up to 16 GPa and 900 K and thermal expansion coefficients under high-pressure conditions were obtained from the EoS. Obtained values of $-\alpha V$, which is the same as pressure dependence of entropy, show that the hydrogen motion certainly affects the lattice system. It is likely that the number of the secondary OH bonding increases from around 2 GPa and does not change beyond 8 GPa at 300 K .

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[^1]:    ${ }^{\text {a }}$ Figures in parentheses indicate estimated standard deviations of the last significant digit

[^2]:    ${ }^{\text {a }}$ Thermal expansion coefficient is expressed as $\alpha=\alpha_{0}+\alpha_{1} T$. Redfern and Wood (1992) originally reported it as $\alpha=\alpha_{0}+\alpha_{1}(T-273)$
    ${ }^{\mathrm{b}}$ Figure in parentheses indicates estimated standard deviations of the last significant digit

[^3]:    ${ }^{\text {a }}$ PXD Powder X-ray diffraction
    ${ }^{\mathrm{b}}$ PND Powder neutron diffraction
    ${ }^{\text {c }}$ SCXD Single-crystal X-ray diffraction
    ${ }^{\mathrm{d}}$ B Brillouin scattering

