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## Heat capacity of wadeite-type $K_2Si_4O_9$ and the pressure-induced stable decomposition of K-feldspar

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**Abstract** The heat capacity of synthetic, stoichiometric wadeite-type  $K_2Si_4O_9$  has been measured by DSC in the  $195 \leq T(K) \leq 598$  range. Near the upper temperature limit of our data, the heat capacity observed by DSC agrees with that reported by Geisinger et al. (1987) based on a vibrational model of their infrared and Raman spectroscopic data. However, with decreasing temperature, the  $C_p$  observed by DSC is progressively higher than that predicted from the vibrational model, suggesting that the standard entropy of  $K_2Si_4O_9$  is likely to be larger than  $198.9 \pm 4.0$  J/K · mol computed from the spectroscopic data. A fit to the DSC data gave:  $C_p(T) = 499.13 (\pm 1.87) - 4.35014 \cdot 10^3 (\pm 3.489 \cdot 10^1) \cdot T^{-0.5}$ , with  $T$  in K and average absolute percent deviation of 0.37%. The room-temperature compressibilities of kalsilite and leucite, hitherto unknown, have been measured as well. The data, fitted to the Murnaghan equation of state, gave  $K_o = 58.6$  GPa,  $K'_o = 0.1$  for kalsilite and  $K_o = 45$  GPa,  $K'_o = 5.7$  for  $\alpha$ -leucite. Apart from the above mentioned data on the properties of the individual phases, we have also obtained reaction-reversals on four equilibria in the system  $K_2O-Al_2O_3-SiO_2$ . The Bayesian method has been used simultaneously to process the properties of 13 phases and 15 reactions between them to derive an internally consistent thermodynamic dataset for the  $K_2O-Al_2O_3-SiO_2$  ternary. The enthalpy of formation of  $K_2Si_4O_9$  wadeite is in perfect agreement with its revised calorimetric value, the standard entropy is  $232.1 \pm 10.4$  J/K · mol,  $\sim 15\%$

higher than that implied by vibrational modeling. The phase diagram, generated from our internally consistent thermodynamic dataset, shows that for all probable  $P$ - $T$  trajectories in the subduction regime, the *stable* pressure-induced decomposition of K-feldspar will produce coesite + kalsilite rather than coesite + kyanite +  $K_2Si_4O_9$  (cf. Urakawa et al. 1994).

### Introduction

Kinomura et al. (1975) first suggested that, with increasing pressure, K-feldspar decomposes to coesite, kyanite, and the compound  $K_2^{[VI]}Si[Si_3O_9]$ . They also demonstrated that the latter compound is isostructural with the naturally occurring mineral wadeite,  $K_2^{[VI]}Zr[Si_3O_9]$ , the Si in octahedral site substituting for Zr. For the sake of convenience, we shall dub the Si-analogue of wadeite as “Si-wadeite” (SWd for short). Occurrence of Si in both six- and four-fold sites being a novelty at that time, SWd drew the interest of a number of workers. Swanson and Prewitt (1983) solved its crystal structure, while Swanson and Prewitt (1986) and Ross et al. (see Geisinger et al. 1987) reported on its volume equation of state. Geisinger et al. (1987) performed calorimetry and came up with its enthalpy of formation. They also calculated its standard entropy and superambient heat capacity based on vibrational models of infrared and Raman spectroscopic data. These data, along with those from Robie et al. (1978), permitted them to compute the  $P$ - $T$  curve for the equilibrium coesite (Cs) + kyanite (Ky) + Si-wadeite (SWd) = 2 K-feldspar (Kfs). Their calculated  $P$ - $T$  curve agreed with the synthesis data of Kinomura et al. (1975) for Kfs on the one hand and the assemblage Cs + Ky + SWd on the other.

More recently, Urakawa et al. (1994) reversed the equilibrium Cs + Ky + SWd = 2 Kfs by in-situ synchrotron radiation study. Their reversed  $P$ - $T$  curve did *not* agree with that computed by Geisinger et al. (1987); however, they gave no explanation for this disparity. In the meanwhile, a revised value for the enthalpy

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of formation of SWd has become available (A. Navrotsky, personal communication 1996). Also available are Robie and Hemingway's (1995) thermodynamic data tables, which are stated to have "entirely superseded" the previous edition (Robie et al. 1978), based on which Geisinger et al. (1987) performed their calculations. While the enthalpy of formation for  $K_2O$  remained unchanged, those for a number of K-bearing phases (including K-feldspar) have undergone substantial revision in Robie and Hemingway (1995). If the Urakawa et al. (1994) reversals were to be correct, and likewise the standard entropy and the superambient  $C_p(T)$  computed by Geisinger et al. (1987) from their vibrational model, Bayesian analysis (for details, see Olbricht et al. 1994) shows that the standard enthalpy of formation of SWd must be around  $-4328$  kJ/mol, disagreeing with the revised calorimetric value of  $-4301.15 \pm 5.73$  kJ/mol (see Appendix).

The purpose of this paper is to communicate DSC data on the  $C_p(T)$  of SWd, measured in the temperature range 195–598 K, which help resolve the above mentioned discrepancy. Another objective of the present study is to undertake a Bayesian analysis of the system  $K_2O-Al_2O_3-SiO_2$ , including most phases of relevance to high-pressure mineral equilibria. The phases to be examined are:  $\alpha$ -quartz (aQz),  $\beta$ -quartz (bQz), coesite (Cs), stishovite (Stv), andalusite (And), sillimanite (Si), kyanite (Ky), corundum (Co), kalsilite (Kls),  $\alpha$ -leucite (aLc),  $\beta$ -leucite (bLc), K-feldspar (Kfs), and Si-wadeite (SWd). For these phases, most information required for a Bayesian study are already available. By contrast, insufficient thermodynamic data are available for  $KAlSi_3O_8$ -hollandite; we had to omit it for now from our list. In addition, we have sought to fill up a few gaps by giving new data on the compressibility of kalsilite and leucite. Some phase equilibria reversals have also been made to supplement the existing database and to verify the calculated phase relations. Finally, an internally consistent thermodynamic dataset has been derived, which allows computation of phase equilibria in the  $K_2O-Al_2O_3-SiO_2$  system. In particular, we shall focus on the stable, pressure-induced decomposition of leucite and K-feldspar. It will be shown that for all reasonable  $P$ - $T$  gradients within the subduction zone, the stable decomposition of K-feldspar leads to the assemblage coesite + kalsilite. By contrast, the stable decomposition of K-feldspar to Si-wadeite + kyanite + coesite is restricted to somewhat lower temperatures, which are of little consequence for the depths of the earth.

## Experimental methods

The experimental techniques required for this work are familiar to most readers; therefore, they will only very briefly be documented.

To synthesize starting materials for determining phase properties (such as compressibility of kalsilite and leucite and molar heat capacity of Si-wadeite) and for reversing several equilibria indicated later, standard cold-seal pressure vessels and an end-loaded piston-cylinder apparatus fitted with "zero friction" NaCl-graphite assemblies of 1.28 and 0.8 cm diameter were used. For the cold-seal apparatus, the uncertainties of  $P$  and  $T$ , due to calibration, gradient and control, are  $\pm 5\%$  of  $P$  and  $\pm 10^\circ C$ . The solid-media apparatus with the 1.28 cm assembly has been most recently calibrated (by T. Fockenberg, personal communication) both at ambient and at elevated temperatures. The room-temperature calibration depended on the Bi I–II transition; at higher temperatures, the calibrations relied on farringtonite to  $Mg_3(PO_4)_2$ -II (Brunet and Vielzeuf 1996) and  $\alpha$ -quartz to coesite transitions. At pressures above 5.5 GPa, the 0.8 cm diameter solid-media cell had to be used. B. Wunder has calibrated this assembly at 1050 °C against the  $CaGeO_3$  garnet to perovskite transition (Susaki et al. 1985). In no case could a perceptible friction loss be detected. The cumulative uncertainty for  $P$  and  $T$  in the 5–6.5 GPa and 700–1000 °C range has been estimated as  $\pm 0.2$  GPa and  $\pm 15^\circ C$ . For the solid-media runs conducted in the  $T$ - $P$ -range between 900–1050 °C and 1.3–1.6 GPa, the uncertainties are believed to be  $\pm 10^\circ C$  and  $\pm 0.05$  GPa.

Gels and glass starting materials, prepared from pure chemicals, were used for synthesizing the phases of interest. While the gels were prepared from  $Si(OC_2H_5)_4$ , Al powder, and  $KHCO_3$  by the technique of Hamilton and Henderson (1968), preparation of the  $K_2O \cdot 4SiO_2$  glass for the synthesis of Si-wadeite followed a slightly modified method originally described by Goranson and Kracek (1932). The starting material, a homogenized mixture of  $KHCO_3$  and  $SiO_2$  of 2:4 molar ratio with 0.24 wt% of excess K, was first slowly heated to 800 °C. After about 24 h, the temperature was slowly raised to 1100 °C. After another 24 h, the melt was quenched to an optically homogeneous glass. Table 1, reproduced later, gives an overview of the starting materials and the synthesis conditions for the individual phases. In all cases, single-phase materials could be prepared. They have been characterized by X-rays, and in one case (SWd) by electron-probe microanalysis (EPMA) as well as  $^{29}Si$  MAS-NMR spectrometry. The X-ray diffraction data for the determination of the lattice parameters were collected using Si (NBS standard reference material 640) as an internal standard. Least squares refinement of the data was done using the computer program by Appleman and Evans (1973); indexing the diffraction lines was invariably guided by calculated intensities. Table 2 lists the lattice parameters. The EPMA was executed on a Cameca SX 50 device. The working conditions were: accelerating voltage 15 kV, beam current 10 nA, beam diameter 8  $\mu m$ , counting time 10 s for peak and background. To guard against loss of K, the beam was slowly swivelled around the point to be analyzed. The standard used was a synthetic K-, Mg-, Ca-, and Al-bearing silicate glass. The  $^{29}Si$  MAS-NMR spectrum of SWd was obtained on a Bruker NMR-spectrometer operated at a resonance frequency of 79.5 MHz, assuming a rather high relaxation time of 300 s for the Si nucleus. The  $^{29}Si$  MAS-NMR spectrum will be reported relative to the TMS standard.

**Table 1** Details of synthesis of various phases

Phase	Starting material	$P$ (GPa)	$T$ ( $^\circ C$ )	Run duration (days)
K-feldspar	Gel	0.2	700	2
Kalsilite	Gel	0.05	800	7
Leucite	Gel	0.05	800	4
Coesite	Glass	3.5	1000	1
Kyanite	Gel	4.5	700	1
"Si-wadeite"	Glass	2.5	700	2

**Table 2** Lattice parameters of some of the synthetic phases. The quantities in parentheses represent one standard deviation; they apply to the last digit(s) of the preceding number

Phase	Space group	a (Å)	b (Å)	c (Å)	$\beta$ (°)	V (Å <sup>3</sup> )
K-feldspar	C2/m	8.6013(12)	13.0279(17)	7.1814(10)	116.01(1)	723.23(12)
Kalsilite	P6 <sub>3</sub>	5.1627(3)		8.7115(6)		201.08(2)
Leucite	I4 <sub>1</sub> /a	13.0556(6)		13.7560(11)		2344.66(23)
“Si-wadeite”	P6 <sub>3</sub> /m	6.6126(9)		9.5101(6)		360.13(3)

Compressibility data for kalsilite and leucite were obtained by in-situ experiments to about 6.1 GPa using the synchrotron radiation facility at HASYLAB, Hamburg. The MAX-80 device, interfaced with a synchrotron source, uses NaCl as an internal pressure calibrant, the equation of state of NaCl (Decker 1966) serves to compute the pressure at each experimental point. On the whole, the standard deviation of  $P$  is judged to be about  $\pm 0.2$  GPa in that pressure range. The initial compression of the sample at room temperature gave diffraction patterns with broad lines and poor resolution due to the development of deviatoric stress in the pressure medium. Fortunately, stress release was achieved by a short heating of the sample at high pressures to near 500 °C. On subsequent decompression, the pressure medium behaved in a quasihydrostatic fashion. The  $P$ - $V$  data collected under near-hydrostatic condition were fitted to the Murnaghan equation of state. Table 3 reproduces these data.

The  $C_p(T)$  data for Si-wadeite was obtained by D.W. Fasshauer under the supervision of G.W.H. Höhne at the Calorimetry laboratory of the University of Ulm. Two Perkin-Elmer scanning calorimeters, DSC-2 and DSC-7, were used to measure the  $C_p(T)$  in the temperature ranges 195–330 K and 313–598 K, respectively. Their temperature and heat-flow rate calibrations were accomplished following the recommendations of Höhne et al. (1990) and Sarge et al. (1994). Synthetic SWd, predried at 120 °C, was weighed into Al pans fitted with crimped lids. Sample sizes were 18–25 mg. The determination of the base line made use of identical pan-lid combinations differing less than 0.005 mg from those with the samples. A sapphire single crystal, weighing 129.642 mg, served as reference. The  $C_p$  of sapphire was taken from Sarge et al. (1994); it is known to 0.4–0.1% and 0.1–0.2% in the ranges 70–300 K and 290–2250 K, respectively. The heating rate for the measurements, alternately executed on the sample and the standard, was 10 K/min. The measurements were carried out in the interval-scanning mode. Table 4 lists the molar  $C_p$  data.

**Table 3** Experimental data on room-temperature compressibility of kalsilite and leucite

Kalsilite		Leucite	
Pressure [GPa]	Cell volume [Å <sup>3</sup> ]	Pressure [GPa]	Cell volume [Å <sup>3</sup> ]
0.0001	201.08	0.0001	2344.66
1.2230	197.10	1.1150	2308.84
2.1300	194.28	2.0210	2246.61
1.6060	195.66	1.0820	2290.17
2.4490	193.09	1.7440	2257.14
3.5910	189.26	1.3920	2277.03
4.6690	185.05	2.3210	2228.44
4.2510	187.91	1.7960	2264.20
5.2680	182.40	2.5140	2248.79
6.1400	179.86	3.5910	2188.09
		3.5910	2199.05
		4.6760	2150.48
		5.7460	2132.67
		5.1000	2155.75
	$K_o$ [GPa] = 58.6		$K_o$ [GPa] = 45.0
	$K_o'$ = 0.1		$K_o'$ = 5.7

## Experimental results

### Characterization of the synthetic phases

The phases of interest to this study were synthesized from appropriate starting materials under various  $P$ - $T$  conditions. Table 1 summarizes the synthesis data. Optical and X-ray diffraction studies showed that each synthesis yielded single-phase material.

Table 2 documents the lattice constants of some of the synthetic phases. They are in excellent agreement with literature values. Following Kroll and Ribbe (1983, Eq. 10a, p. 77), the lattice constants of the K-feldspar (sanidine) translate to an Al-occupancy of each T1 site of 0.2942. That corresponds to the non-convergent ordering parameter  $Q_t$  (as defined by Carpenter and Salje, 1994) of 0.177. Based on the  $T$ -dependence of  $Q_t$  (see Fig. 5 in Carpenter and Salje, 1994), our synthetic Kfs was slightly more disordered than what would be expected in the event of internal equilibrium. Besides X-rays, our synthetic Si-wadeite was characterized by EPMA and <sup>29</sup>Si MAS-NMR spectrometry. The average of 12 EPMA on SWd grains of 20–50  $\mu$ m diameter gave  $K_{1.991(\pm 0.012)}Si_{4.003(\pm 0.003)}O_9$ , indicating that our synthetic Si-wadeite was of stoichiometric composition. Its NMR spectrum comprised two sharp peaks at –95.0 (for <sup>[IV]</sup>Si) and –203.1 ppm (for <sup>[VI]</sup>Si); they had the same intensity ratios as reported by Stebbins and Kanzaki (1991).

### Room-temperature compressibilities of kalsilite and leucite

Table 3 lists the pressure versus cell volume data obtained for kalsilite and leucite, respectively, at ambient temperature in a quasi-hydrostatic medium using a MAX-80 device interfaced to a synchrotron source. The data have been smoothed by Murnaghan equation of state. The bulk modulus  $K_o$  and its pressure-derivative,  $K_o'$  are indicated at the bottom of the table. As far as we are aware, no previous data on these quantities exist in the literature.

### Molar heat capacity of Si-wadeite

The heat capacity of synthetic Si-wadeite could successfully be measured in the temperature range 195–598 K. Viewed under the microscope, the Si-wadeite sample

**Table 4** DSC data on the molar heat capacity for Si-wadeite (SWd)

$T$ (K)	$C_p$ (J/mol · K)	Wt	$T$ (K)	$C_p$ (J/mol · K)	Wt	$T$ (K)	$C_p$ (J/mol · K)	Wt	$T$ (K)	$C_p$ (J/mol · K)	Wt
195.00	186.83	1.0	305.00	250.63	1.0	393.08	284.35	0.0	488.22	309.65	0.0
200.00	190.23	1.0	310.00	253.50	1.0	378.23	277.21	0.5	498.22	310.15	0.0
205.00	194.71	1.0	315.00	255.59	0.5	388.23	281.10	1.0	508.22	310.27	0.0
210.00	197.63	1.0	320.00	258.15	0.5	398.23	282.03	1.0	513.22	310.47	1.0
215.00	202.26	1.0	325.00	258.50	0.5	403.23	282.92	1.0	518.22	310.34	1.0
220.00	204.36	1.0	330.00	261.13	0.5	408.23	284.01	1.0	523.22	310.52	1.0
225.00	208.86	1.0	313.28	250.11	0.0	413.23	285.05	1.0	528.22	310.61	1.0
230.00	211.56	1.0	318.22	253.02	0.5	418.23	285.97	1.0	533.22	310.37	1.0
235.00	215.32	1.0	323.28	255.47	0.5	423.23	286.53	1.0	538.22	310.27	1.0
240.00	218.23	1.0	328.22	257.79	0.5	428.23	287.89	1.0	543.22	310.61	1.0
245.00	222.01	1.0	333.28	259.71	0.5	433.22	289.84	1.0	548.22	311.17	1.0
250.00	224.69	1.0	338.21	261.83	1.0	438.22	290.78	1.0	553.22	312.07	1.0
255.00	226.60	1.0	343.28	263.94	1.0	443.22	291.53	1.0	558.22	313.36	1.0
260.00	230.46	1.0	348.21	265.85	1.0	448.22	292.24	1.0	563.22	314.91	1.0
265.00	231.92	1.0	353.28	267.98	1.0	453.22	292.82	1.0	568.22	316.83	1.0
270.00	234.52	1.0	358.21	269.96	1.0	458.22	293.86	1.0	573.21	319.68	1.0
275.00	236.61	1.0	363.28	271.68	1.0	463.22	294.91	1.0	578.21	322.81	0.0
280.00	240.43	1.0	368.21	273.79	1.0	468.22	296.09	1.0	588.21	331.08	1.0
285.00	241.80	1.0	373.28	275.69	1.0	473.22	297.99	1.0	578.24	317.63	1.0
290.00	244.05	1.0	378.21	277.76	0.5	478.22	300.06	1.0	583.24	318.76	1.0
295.00	246.94	1.0	383.28	279.88	0.5	488.22	304.91	1.0	588.24	320.71	1.0
300.00	248.56	1.0	388.21	282.11	0.0	478.22	309.23	0.0	593.24	322.77	1.0
									598.24	325.26	0.0

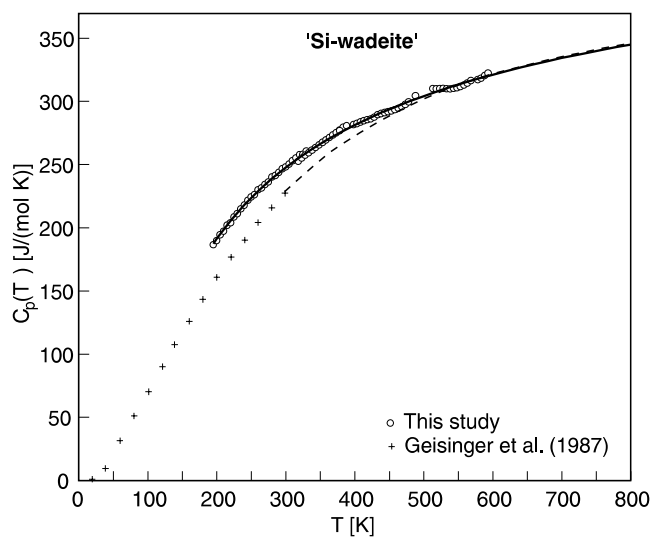
shows xenomorphic to hypidiomorphic crystals having an average grain size of  $10 \times 20 \mu\text{m}$ , ranging up to  $20 \times 60 \mu\text{m}$ . Table 4 lists the  $T$  versus  $C_p$  data. While data scatter was barely a problem, “offsets” of data (very similar to that documented by Komada et al. 1995, Figs. 2 and 7) at the beginning and at the end of each scanning interval increased with rising temperature. Above 593 K, data “offset” and scatter became too strong to permit reliable  $C_p$  measurement. The X-ray diffractogram of Si-wadeite exposed to a  $T$  slightly above 600 K did not reveal any damage to the sample, nor could any change be observed on an SEM image; thus no obvious explanation for the “offsets” seems to exist. The overall uncertainty of the data is believed to be 1%. Smoothing these data by a least squares fit made use of all datapoints with a percent deviation less than about 1%, eliminating very few “offsets”. All datapoints were assigned unit weight, excepting those in the regions of overlap of the scanning intervals, which were weighted 0.5. The  $C_p(T)$  function recommended by Berman and Brown (1985) was used. Of the four fit parameters, only two were adequate to represent the data:  $C_p(T) = 499.13 (\pm 1.87) - 4.35014 \cdot 10^3 (\pm 3.489 \cdot 10^1) \cdot T^{-0.5}$ , with  $T$  given in (K). The average absolute percent deviation of the fit is 0.37%.

It is interesting to compare the DSC data for  $C_p(T)$  of SWd with that computed from a vibrational model of infrared and Raman spectra by Geisinger et al. (1987). Near the upper temperature limit of the DSC measurement, they are essentially identical. However, at lower temperatures, the DSC data are progressively higher. Figure 1 depicts the two sets of data; it is clear that the lower the temperature, the greater the difference between the two. Thus, it seems likely that the standard entropy

of SWd will be higher than that given by Geisinger et al. (1987).

#### Experimental reversal of some equilibria

A few reversals for the equilibria  $\text{Kls} + \text{Kfs} = \text{aLc}$ ,  $\text{Kls} + \text{Kfs} = \text{bLc}$ ,  $\text{SWd} + \text{Ky} + \text{Cs} = \text{Kfs}$  have been



**Fig. 1** Comparison of the heat capacity of “Si-wadeite” obtained by DSC (circles) with those calculated from a vibrational model of infrared and Raman spectroscopic data by Geisinger et al. (1987). In the “low-temperature” range the  $C_p$  data by Geisinger et al. are shown as crosses, their superambicent  $C_p(T)$  function by the dashed line. The two parameter  $C_p(T)$  fit to our DSC data is represented by the solid line

achieved by us to supplement the existing database. A preliminary Bayesian analysis of all phase property and phase equilibria data of the system  $\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$  gave a set of internally consistent thermodynamic data for the 13 phases of relevance to this study. The  $P$ - $T$  diagram computed from this “preliminary” set of internally consistent thermodynamic data suggested that  $\text{SWd} + \text{Ky} + \text{Cs} = \text{Kfs}$  will become metastable above 500 °C; at higher temperatures, the stable equilibrium will be  $\text{Kls} + \text{Cs} = \text{Kfs}$ . That has been confirmed by reversing the  $\text{Kls} + \text{Cs} = \text{Kfs}$  equilibrium. Tables 5a through 5d document the critical reversal runs. Attention is drawn to the slight but definite change in the order parameter,  $Q_t$ , of the Kfs during the runs; they indicate a tendency toward achievement of internal equilibrium in the Kfs in course of the runs.

In a subsequent cycle, the complete set of phase property and phase equilibria restrictions from the literature, along with those obtained by us, was processed by the Bayesian method; that led to the “final” internally consistent thermodynamic dataset for the 13 phases of the  $\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$  system, presented later on in Table 8.

### The refined thermodynamic dataset for the phases of the $\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$ system

#### The Bayesian approach

To handle simultaneously the phase properties (like standard enthalpies of formation, standard entropies etc.) and phase equilibria restrictions, the Bayesian ap-

proach, described in detail by Olbricht et al. (1994), has been adopted. The quality of results obtained by the Bayes method has been illustrated earlier on several occasions (e.g., Chatterjee et al. 1994; Waterwiese et al. 1995; Fasshauer et al. 1997). Only a very brief account of the method needs to be given here. In the Bayesian method, the phase properties (like standard molar enthalpy of formation,  $H_{f,T^\circ}^\circ$ , molar entropy,  $S_{T^\circ}^\circ$ , molar heat capacity,  $C_p(T)$ , standard molar volume,  $V_{T^\circ}^\circ$ , the temperature-dependence of molar volume  $V^\circ(T)$ , bulk modulus and its pressure-derivative,  $K_o$  and  $K_o'$ ) of each phase is combined with the reaction properties ( $\Delta\mu > 0$  for stable reactants and  $\Delta\mu < 0$  for stable products) of all reactions between the phases to derive a set of “refined” thermodynamic data, together with their uncertainties and correlations. The term  $\Delta\mu$  follows from the relation

$$\Delta\mu = \sum_i v_i \mu_i \quad (1)$$

where  $v_i$  and  $\mu_i$  stand for the stoichiometric coefficient and chemical potential of the  $i$ -th phase component, respectively, the products counting positive and the reactants negative. Because we are concerned with end-member phases in the present context, we may write the chemical potential of the  $i$ -th substance,  $\mu_i$ , as

$$\mu_i = H_{f,T^\circ,i}^\circ - T \cdot S_{T^\circ,i}^\circ + \int_{T^\circ}^T C_{p,i}(T) dT - T \cdot \int_{T^\circ}^T (C_{p,i}(T)/T) dT + \int_{P^\circ}^P V_i(T,P) dP + G_{tr,i} \quad (2)$$

**Table 5a** Run data on the reversal of the equilibrium 1 Kls + 1 Kfs = 2 aLc

$T$ (°C)	$P$ (GPa)	Run time(h)	Run products	$Q_t$ (starting Kfs)	$Q_t$ (product Kfs)
520	0.20	2975	Kfs + Kls increase	0.177	0.216
605	0.40	913	Kfs + Kls increase	0.177	0.212
625	0.40	861	Lc increases	0.177	–

**Table 5b** Run data on the reversal of the equilibrium 1 Kls + 1 Kfs = 2 bLc

$T$ (°C)	$P$ (GPa)	Run time(h)	Run products	$Q_t$ (starting Kfs)	$Q_t$ (product Kfs)
899	1.50	113	Kfs + Kls increase	0.177	0.168
928	1.31	137	Lc increases	0.177	–
1058	1.60	44	Lc increases	0.177	–

**Table 5c** Run data on the reversal of the equilibrium 1 SWd + 1 Ky + 1 Cs = 2 Kfs

$T$ (°C)	$P$ (GPa)	Run time(h)	Run products	$Q_t$ (starting Kfs)	$Q_t$ (product Kfs)
800	6.30	96	Kfs decreases	0.177	–
800	6.10	96	No reaction	0.177	–
800	5.90	96	Kfs increases	0.177	Not determined

**Table 5d** Run data on the reversal of the equilibrium 1 Kls + 2 Cs = 1 Kfs

$T$ (°C)	$P$ (GPa)	Run time(h)	Run products	$Q_t$ (starting Kfs)	$Q_t$ (product Kfs)
700	5.30	96	No reaction	0.177	–
700	5.50	168	Kls + Cs increase	0.177	–
1000	5.50	24	Kfs increases	0.177	0.237

with  $V_i(T,P)$ , indicating the  $T$ - $P$ -dependence of the molar volume of  $i$  and  $G_{ir,i}$ , the molar Gibbs energy of phase transition of  $i$ , if there is one in the range  $T^\circ$  to  $T$  and  $P^\circ$  to  $P$ . The reference temperature and pressure,  $T^\circ$  and  $P^\circ$ , are defined as 298.15 K and 1 bar, respectively. The  $T$ -dependence of the molar volume,  $V^\circ(T)$ , will be expressed as

$$V^\circ(T) = V_{T^\circ}^\circ \cdot (1 + v_1 \cdot (T - T^\circ) + v_2 \cdot (T - T^\circ)^2) \quad (3)$$

The  $P$ -dependence of the molar volume will be treated in terms of the Murnaghan equation. As such,  $V(T,P)$  of Eq. (2) at any set of  $T$  and  $P$  will be given by the expression

$$V(T,P) = V^\circ(T) \cdot \left(1 + \frac{K'_o}{K_o} \cdot P\right)^{-\frac{1}{K'_o}} \quad (4)$$

$K_o$  and  $K'_o$  being the room-temperature bulk modulus and its pressure-derivative, respectively. Of the various phase properties, only  $H_{f,T^\circ}^\circ$ , and  $S_{T^\circ}^\circ$  will be regarded as variables; therefore, only they need to be refined (i.e. updated subject to the reaction property restrictions,

$\Delta\mu > 0$  or  $\Delta\mu < 0$ ), all other quantities will be handled as  $T,P$ -dependent “constants”. In other words, the refined set of thermodynamic data will comprise  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$  for each phase, as well as their uncertainties and correlations. It may be pointed out that the Bayesian technique has to deal with the same two quantities also handled by mathematical programming; however only the former returns the uncertainties for  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$  and the correlations between them. For an extensive treatment of the relative merits of the two methods, the reader is referred to Olbricht et al. (1994).

#### Phase property data

Table 6 summarizes the sources of the phase property data used as input in our Bayesian analysis.  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$  of most phases are known; in a few cases they had to be estimated. In the Bayes method, the former categories of  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$  are handled as normally distributed

**Table 6** Sources of the phase property data used as input in Bayes analysis. The reference phases are marked with *asterisks*. Estimated quantities are indicated by the symbol  $\otimes$

Phase	$H_{f,T^\circ}^\circ$	$S_{T^\circ}^\circ$	$C_p(T)$	$V_{T^\circ}^\circ$	$V^\circ(T)$	$K_o, K'_o$
Andalusite	[1]	[1]	[1]	[2]	[3]	[4]
Corundum*	[5]	[5]	[1]	[1]	[3]	[6]
Coesite	[7]	[7]	[7]	[3]	[3]	[8]
K-Feldspar*	[1]	[1]	[9]	[10]	[3]	[11]
Kalsilite	$\otimes$ [1]	[1]	[9], [12]	[1]	[13]	[14]
Kyanite	[1]	[1]	[1]	[2]	[3]	[15]
“Si-wadeite”	[16]	$\otimes$ [14]	[14]	[17]	[18]	[18]
Sillimanite	[1]	[1]	[1]	[2]	[19]	[3]
Stishovite	[7]	[7]	[7]	[20], [21]	[20], [21]	[8]
$\alpha$ -Leucite	$\otimes$ [1]	[1]	[22], [23], [24]	[25]	[25]	[14]
$\alpha$ -Quartz*	[5]	[5]	[9], [3]	[1]	[3]	[8]
$\beta$ -Leucite	$\otimes$ [14]	$\otimes$ [14]	[22], [23], [24]	[25]	[25]	$\otimes$ [14]
$\beta$ -Quartz	$\otimes$ [26]	$\otimes$ [27]	[9]	[3]	[3]	[3]

[1] Robie, Hemingway (1995); [2] Holdaway, Mukhopadhyay (1993); [3] Berman (1988); [4] Ralph et al. (1984); [5] Cox et al. (1989); [6] Richet et al. (1988); [7] Akaogi et al. (1995); [8] Hemley et al. (1994); [9] Berman, Brown (1985); [10] Kroll et al. (1986); [11] Angel (1994); [12] Berman, Brown (1986); [13] Henderson, Taylor (1988); [14] This study; [15] Comodi et al. (1997); [16] A. Navrotsky (personal communication); [17] Swanson, Prewitt (1983); [18] Geisinger et al. (1987); [19] Hemingway et al. (1991); [20] Ito et al. (1974); [21] Endo et al. (1986); [22] Kelley et al. (1953); [23] Pankratz (1968); [24] Lange et al. (1986); [25] Palmer et al. (1989); [26] Chermak, Rimstidt (1989); [27] Holland (1989)

**Table 7** Sources of the reaction reversal data used as input in Bayesian analysis

Reversed equilibria	Sources
1 Ky = 1 And	Bohlen et al. (1991), Newton (1966b), Richardson et al. (1969), Holdaway (1971)
1 And = 1 Si	Holdaway (1971), Heninger, Bowman (both in Holdaway and Mukhopadhyay 1993), Weill (1966)
1 Ky = 1 Si	Newton (1966a), Bohlen et al. (1991), Richardson et al. (1968)
1 aQz = 1 bQz	Mirwald and Massonne (1980)
1 Cs = 1 aQz	Bohlen and Boettcher (1982)
1 Cs = 1 bQz	Mirwald and Massonne (1980)
1 And = 1 Co + 1 aQz	Harlov and Newton (1990)
1 Ky = 1 Co + 1 bQz	Harlov and Newton (1993)
1 Stv = 1 Cs	Zhang et al. (1996)
1 Co + 1 Stv = 1 Ky	Schmidt et al. (1997)
1 SWd + 1 Ky + 1 Cs = 2 Kfs	Urakawa et al. (1994), This study (Table 5c)
1 Kls + 1 Kfs = 2 aLc	Scarfe et al. (1966), This study (Table 5a)
1 Kls + 1 Kfs = 2 bLc	Scarfe et al. (1966), Lindsley (1966), This study (Table 5b)
1 aLc = 1 bLc	Lange et al. (1986)
1 Kls + 2 Cs = 1 Kfs	This study (Table 5d)

**Table 8** Refined thermodynamic data for phases of the  $K_2O-Al_2O_3-SiO_2$  system compared to the calorimetric input data used in Bayesian work. The numbers in parentheses are 2 standard deviations for the preceding quantity. Asterisks identify the reference phases

Phase	Composition	Abbreviation	$H_{f,T^\circ}^\circ$ [J/mol] (input)	$H_{f,T^\circ}^\circ$ [J/mol] (refined)	$S_{T^\circ}^\circ$ [J/K · mol] (input)	$S_{T^\circ}^\circ$ [J/K · mol] (refined)
Andalusite	$Al_2O(SiO_4)$	And	-2589900(2000)	-2589873(493)	91.40(0.50)	91.508(0.417)
Corundum*	$Al_2O_3$	Co	-1675700(1300)	-1675700(0)	50.92(0.10)	50.917(0.100)
Coesite	$SiO_2$	Cs	-907300(1200)	-907033(173)	40.70(1.00)	40.727(0.192)
K-feldspar*	$K[AlSi_3O_8]$	Kfs	-3974600(3900)	-3974600(0)	214.20(0.40)	214.273(0.388)
Kalsilite	$K[AlSiO_4]$	Kls	-	-2123846(2401)	133.30(1.20)	133.615(1.146)
Kyanite	$Al_2O(SiO_4)$	Ky	-2593800(2000)	-2593856(458)	82.80(0.50)	82.790(0.367)
“Si-wadeite”	$K_2Si[Si_3O_9]$	SWd	-4301150(5730)	-4301136(5646)	-	232.107(10.447)
Sillimanite	$Al_2O(SiO_4)$	Si	-2586100(2000)	-2586287(454)	95.40(0.50)	95.372(0.384)
Stishovite	$SiO_2$	Stv	-873700(1600)	-872121(1224)	27.30(1.00)	26.202(0.698)
$\alpha$ -Leucite	$K[AlSi_2O_6]$	aLc	-	-3029582(1266)	200.20(1.70)	198.438(1.104)
$\alpha$ -Quartz*	$SiO_2$	aQz	-910700(1000)	-910700(0)	41.46(0.20)	41.467(0.109)
$\beta$ -Leucite	$K[AlSi_2O_6]$	bLc	-	-3023444(1498)	-	205.486(1.036)
$\beta$ -Quartz	$SiO_2$	bQz	-	-908595(83)	-	44.251(0.145)

quantities with known expectation values and variances, by contrast, the estimated quantities are treated as uniformly distributed. As stated earlier, of all the quantities in Table 6, only  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$  will be refined subject to the phase equilibria restrictions, excepting the reference  $H_{f,T^\circ}^\circ$  of one phase per system component. The reference phases will be Kfs, Co and aQz; their  $H_{f,T^\circ}^\circ$  will emerge unmodified in the refined thermodynamic dataset. Not included in Table 6 are the parameters from which the  $G_{tr}$ -term of Eq. (2) has been calculated. For phase transitions in quartz, leucite and kalsilite, the relevant

parameters are given by Berman and Brown (1986) and Berman (1988). Carpenter and Salje’s (1994) Landau formalism, which takes care of the microcline-sanidine transition as well as the non-convergent Al,Si order-disorder in sanidine, has been used to compute  $G_{tr}$  in Kfs.

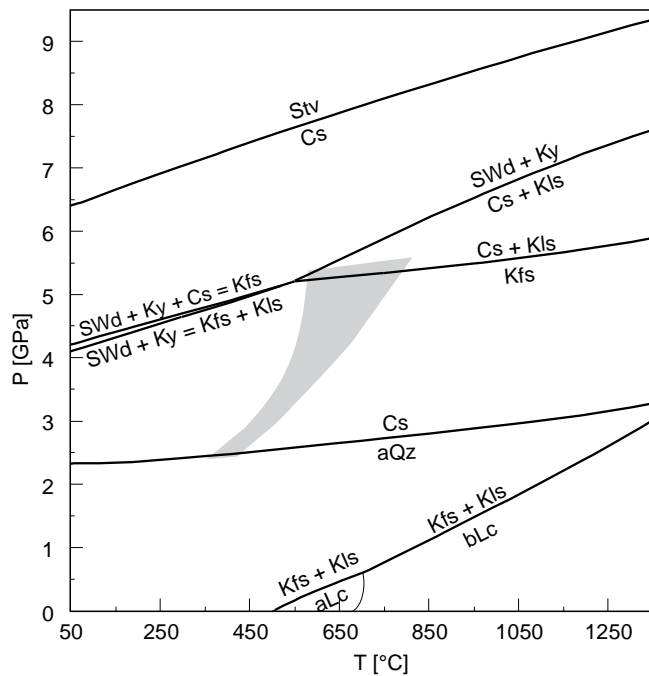
#### Reaction reversal data

Table 7 summarizes the sources of the reaction reversal data culled from the literature. They have been supplemented by our data given above. In all, 15 reactions are considered. In each case, the nominal  $P, T$  reversals have been expanded “away from the equilibrium” using the uncertainty of  $P$  and  $T$  indicated by the authors.

#### Results

Table 8 documents the refined values for  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$  of all phases and their  $2\sigma$  uncertainties; not reproduced, for the sake of brevity, is the correlation matrix. The final values of  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$ , summarized in Table 8, were obtained by the Markov chain Monte Carlo technique called Gibbs sampling (cf. Olbricht et al. 1994).

We wish to focus on several aspects of the refined values of  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$ . First, they overlap with the corresponding input data within  $1-2\sigma$  range. Second, their  $2\sigma$ -uncertainties are now much smaller. Third, the  $H_{f,T^\circ}^\circ$  of the reference phases (flagged by asterisks in Table 8) have not changed. And finally, the  $H_{f,T^\circ}^\circ$  of Si-wadeite is in agreement with its revised value (see thermodynamic cycle reproduced in the Appendix) but its  $S_{T^\circ}^\circ$  is larger than that computed by Geisinger et al. (1987) from their spectroscopic data. The larger  $S_{T^\circ}^\circ$  is compatible with the systematically higher  $C_p$  observed by DSC in the subambient range (Fig. 1) compared to that derived from vibrational spectroscopy. We submit, however, that a calorimetric determination of  $S_{T^\circ}^\circ$  of Si-wadeite will be necessary to verify our value. For now, we may conclude that the DSC data on the  $C_p(T)$  of



**Fig. 2**  $P$ - $T$  diagram based on our refined thermodynamic dataset for the  $K_2O-Al_2O_3-SiO_2$  ternary showing the pressure-induced decomposition of leucite and K-feldspar and the stability fields of  $\alpha$ -quartz, coesite, and stishovite. The stippled area depicts the range of steady-state  $P$ - $T$  paths followed by the top of a subducting oceanic crust for convergence rates between 1 and 10 cm/year (from Peacock et al. 1994)

SWd has helped reconcile phase equilibria in the  $K_2O$ - $Al_2O_3$ - $SiO_2$  ternary with the revised value of  $H_{f,T^\circ}^\circ$  of Si-wadeite.

### Calculated phase relations and discussions

Using the refined values of  $H_{f,T^\circ}^\circ$  and  $S_{T^\circ}^\circ$  (Table 8) and the ancillary phase property data (from sources in Table 6), a  $P$ - $T$  diagram for the system  $K_2O$ - $Al_2O_3$ - $SiO_2$  can be generated. Figure 2 depicts, for clarity, just a few  $P$ - $T$  curves to highlight the pressure-induced disproportionation of K-feldspar and leucite.

The decomposition of K-feldspar to the assemblage SWd + Ky + Cs becomes metastable at about 550 °C. Above that temperature, K-feldspar disproportionates to Cs + Kfs at somewhat lower pressure than the metastable extension of the SWd + Ky + Cs = Kfs curve. A range of  $P$ - $T$  trajectories for subduction regimes (Peacock et al. 1994), shown by stippling in Fig. 2, serves to emphasize that only the decomposition of Kfs

to Cs + Kfs is of relevance to nature. That notwithstanding, it is quite unlikely that pressure-induced decomposition of Kfs to Cs + Kfs will be observed directly in rocks owing to the extremely high pressure required for that process, although coesite (Chopin 1984) and diamond (Sobolev and Shatsky 1990; Shutong et al. 1992) are known from rocks from subduction regimes. By contrast, leucite decomposes to Kfs + Kfs at far lower pressures and has been reported from nature (Deer et al. 1992, p. 484).

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**Appendix:** thermodynamic cycle for the enthalpy of formation of  $K_2^{[IV]}Si[Si_3O_9]$  (SWd) from the stable elements at 298.15 K and 1 bar

Reactions	$\Delta H (\pm 2\sigma)$	Sources, remarks
$K_2Si_4O_9$ (SWd 298 K) = $K_2Si_4O_9$ (SWd glass 973 K)	279.66 (2.98)	Geisinger et al. 1987
$K_2Si_4O_9$ (SWd glass 973 K) = $K_2Si_4O_9$ (solution 973 K)	-21.79 (0.96)	Geisinger et al. 1987
$K_2O$ (crystal 298 K) = $K_2O$ (solution 973 K)	-193.68 (1.10)	Kiseleva et al. 1996
$4SiO_2$ (aQz 298 K) = $4SiO_2$ (solution 973 K)	4[39.10 (0.30)]	Kiseleva et al. 1996
$K_2O$ (crystal 298 K) + $4SiO_2$ (aQz 298 K) = $K_2Si_4O_9$ (SWd 298 K)	-295.15 (3.53)	Formation of SWd from the oxides
$2K + 0.5O_2 = K_2O$ (crystal 298 K)	-363.20 (2.10)	Robie and Hemingway (1995)
$4Si + 4O_2 = 4SiO_2$ (aQz 298 K)	4[-910.7 (1.00)]	Robie and Hemingway (1995)
$2K + 4Si + 4.5O_2 = K_2Si_4O_9$ (SWd 298 K)	-4301.15 (5.73)	Formation of SWd from the elements

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